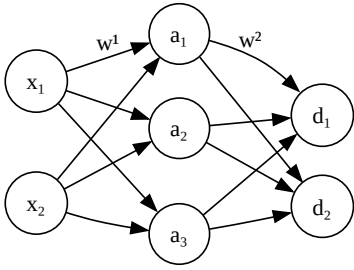

Observations

$$i, j, k, l, L, m, M, n, N, o \in \mathcal{N} \quad (1)$$

$$X \in \mathcal{R}^{n \times o} \quad (2)$$

$$Y \in \mathcal{R}^{n \times m} \quad (3)$$

Neural Network


$$a^0 = x_{1 \times p}(n) \quad (4)$$

$$a^L = d_{1 \times m}(n) \quad (5)$$

$$a^l = \varphi(z^l) \quad (6)$$

$$z^l = a^{l-1}W^l \quad (7)$$

Gradient Descent

$$e(n) = y(n) - d(n) \quad (8)$$

$$\xi(n) = \frac{1}{2}ee^T \quad (9)$$

$$\xi(n) = \frac{1}{2} \sum_{j=1}^M (e_j(n))^2 \quad (10)$$

$$W_{(k+1)} = W_{(k)} - \nabla_W \xi(d, y) \quad (11)$$

$$\xi_{avg}(n) = \frac{1}{2n} \sum_{n=1}^N \sum_{j=1}^M (e_j(n))^2 \quad (12)$$

$$(13)$$

Backpropagation

$$\frac{\partial \xi}{\partial \omega_{ij}^l} = \delta_j^l \frac{\partial z_j^l}{\partial \omega_{ij}^l} \quad (14)$$

$$\delta_j^l = \frac{\partial \xi}{\partial z_j^l} \quad (15)$$

$$\frac{\partial z_j^l}{\partial \omega_{ij}^l} = a_i^{l-1} \quad (16)$$

$$\frac{\partial \xi}{\partial \omega_{ij}^l} = \delta_j^l a_i^{l-1} \quad (17)$$

$$(18)$$

Output Layer

$$\delta_j^L = \frac{\partial \xi}{\partial z_j^L} = \frac{\partial \xi}{\partial a_j^L} \frac{\partial a_j^L}{\partial z_j^L} \quad (19)$$

$$\delta_j^L = \frac{\partial \xi}{\partial a_j^L} \varphi'(z_j^L) \quad (20)$$

$$= -e_j \varphi'(z_j^L) \quad (21)$$

Hidden Layer

$$\delta_j^l = \frac{\partial \xi}{\partial z_j^l} = \sum_k \frac{\partial \xi}{\partial z_k^{l+1}} \frac{\partial z_k^{l+1}}{\partial z_j^l} \quad (22)$$

$$\delta_j^l = \sum_k \delta_k^{l+1} \frac{\partial z_k^{l+1}}{\partial z_j^l} \quad (23)$$

$$\frac{\partial z_k^{l+1}}{\partial z_j^l} = \frac{\partial}{\partial z_j^l} \left(\sum_j \omega_{jk}^{l+1} \varphi(z_j^l) \right) \quad (24)$$

$$\frac{\partial z_k^{l+1}}{\partial z_j^l} = \omega_{jk}^{l+1} \varphi'(z_j^l) \quad (25)$$

$$\delta_j^l = \sum_k \delta_k^{l+1} \omega_{jk}^{l+1} \varphi'(z_j^l) \quad (26)$$

$$(27)$$